

# Distributed Counting along Lossy Paths without Feedback<sup>\*</sup>

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**Abstract.** Network devices need packet counters for a variety of applications. For a large number of concurrent flows, on-chip memories can be too small to support a separate counter per flow. While a single network element might struggle to implement flow accounting on its own, in this work we study alternatives leveraging underutilized resources elsewhere in the network and implement flow accounting on multiple network devices. This paper takes the first step towards understanding the design principles for robust network-wide accounting with lossy unidirectional channels without feedback.

## 1 Background and problem settings

**Scalability challenges.** Per-flow packet counting in network devices is a crucial functionality in network operation, management, and accounting [1–5]. When a packet arrives to a network device that needs to perform per-flow counting, fast-path processing in the device determines the flow associated with the packet and increments the flow counter. Packet counting is traditionally done in a single network device, but it becomes prohibitively expensive—if at all feasible—to maintain per-flow counters as the number of flows and link speeds grow. Proposed solutions either sacrifice counting accuracy or adopt complex memory architectures. Our paper explores an alternative of network-wide packet counting.

**Horizontal vs. vertical counter split.** To count packets in a flow, network devices involved in distributed accounting have to lie on the flow’s path; at the very least, each flow traverses two switches, its source and destination. Assuming reliable communication, a flow counter can be allocated in any one of the network elements in its path; we call this representation a *horizontal split*. In this work, we relax the constraints on interconnecting links as much as possible, assuming an unreliable unidirectional communication without feedback. Then horizontal

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split becomes infeasible since packets can be dropped before they ever reach the counter, so some part of the counter should be allocated on the source network element. We split the counter into two chunks for source and destination switches; we call this a *vertical split*. Since any given switch stores only a fraction of the counter, it needs less memory to support counting the same number of flows. With our relaxed assumptions on interconnecting links, it is crucial to make distributed execution robust to packet reordering and loss; moreover, we also assume that each packet is allowed to carry only a few bits, which can significantly complicate the operation of distributed counters.

**Problem statement.** An asynchronous network delivers a flow  $f$  of packets from source switch  $S$  to destination switch  $D$ , where  $p_i$  is an  $i$ -th packet of  $f$  at  $S$ ,  $i = 0, \dots, |f| - 1$ . Our goal is to compute  $|f|$ , i.e., number of packets received by ingress switch  $S$  from a flow  $f$ . Switches  $S$ ,  $D$  maintain partial counter states of at most  $n$  bits. The proposed distributed counter representations should be able to exactly reconstruct the counter value after a flow terminates; during a flow’s lifetime, counter values returned by queries should not decrease in time and cannot exceed the actual counter value. We study the problem of correctly executing counters under space constraints despite potential packet reordering and loss. We assume that a packet can be prepended by at most  $t$  bits.

## 2 Proposed method

Splitting a counter between source and destination switches is a ubiquitous model since it does not make any assumptions about routing. Robustness of the distributed accounting to packet reordering and loss certainly has its fundamental limits, e.g., the loss of *all* packets in the network disables stateful communication. To characterize the limits of achievable robustness, we represent delivery disruptions with two parameters:

- *reordering parameter*  $R$  is the maximal extent of packet reordering, i.e., the destination switch can receive packet  $p_j$  before packet  $p_i$  only if  $j \leq i + R$ ;
- *loss parameter*  $L$  is the length of a maximal interval of consecutive losses, i.e., the destination switch receives at least one packet from any range  $p_i, \dots, p_{i+L}$ .

To overcome delivery disruptions, both  $S$  and  $D$  use  $t$  bits of the  $n$ -bit counter chunk as *synch bits* to synchronize the two counter chunks. These  $t$  synch bits are the most significant bits in  $S$ ’s chunk  $c_1$ , least significant in  $D$ ’s chunk  $c_2$ , and middle bits in flow  $f$ ’s merged two-chunk counter  $c$ , which counts up to  $2^{2n-t}$ . Upon receiving a packet  $p$ , switch  $S$  records synch bits from its counter  $c_1$  into packet header  $h[p]$  and increments the  $n$ -bit counter. When  $p$  arrives to  $D$ , the latter computes the difference between packet header  $h[p]$  and the  $t$  synch bits in counter  $c_2$ . If this difference is between 1 and  $2^{t-1}$ , switch  $D$  adds it to  $c_2$ . Upon the completion of flow  $f$ , the controller managing accounting network infrastructure collects the  $c_1$  and  $c_2$  values from  $S$  and  $D$  to obtain  $|f|$ , i.e., the total number of flow  $f$ ’s packets received by switch  $S$ : the controller sets the  $n$  most

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**Algorithm 1:** Two-switch counting.
 

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<pre> <b>procedure</b> SOURCEUPDATE(<math>p</math>)     <math>h[p] = c_1 \gg (n - t)</math>     <math>c_1 = (c_1 + 1) \bmod 2^n</math> <b>end procedure</b></pre>	<pre> <b>function</b> DIFFERENCE(<math>a, b, t</math>)     <math>\delta := (a + 2^t - b \bmod 2^t) \bmod 2^t</math>     <b>return</b> <math>\delta</math> <b>end function</b></pre>
<pre> <b>procedure</b> DESTINATIONUPDATE(<math>p</math>)     <math>\text{diff} := \text{Difference}(h[p], c_2, t)</math>     <b>If</b> <math>1 \leq \text{diff} \leq 2^{t-1}</math> <b>then</b>         <math>c_2 := c_2 + \text{diff}</math>     <b>end procedure</b></pre>	<pre> <b>procedure</b> TOTALCOUNT(<math>c_1, c_2</math>)     <math>c := c_2 \ll (n - t)</math>     <math>c := c + \text{Difference}(c_1, c, n)</math> <b>end procedure</b></pre>

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significant bits of counter  $c$  to  $c_2$  and then adds to  $c$  the difference between  $c_1$  and the  $n$  least significant bits of  $c$ . Algorithm 1 consists of the SOURCEUPDATE, DESTINATIONUPDATE, and TOTALCOUNT procedures described above.

**Theorem 1.** *Algorithm 1 correctly counts up to  $2^{2n-t}$  packets under the following conditions:*

$$L + R < 2^{n-1} \quad \text{and} \quad R \leq 2^{n-1} - 2^{n-t}. \quad (1)$$

*Proof.* To prove correctness, we have to show that each update of  $c_2$  by switch  $D$  is correct, i.e.,  $c_2$  becomes equal to  $i \gg (n - t)$  after  $D$  receives any packet that updates  $c_2$ . We prove it by induction. When  $D$  receives its first packet, the packet's index is at most  $L + R$  (this can happen if the first  $L$  packets of the flow are lost, and packet  $p_{L+R}$  arrives to  $D$  first, before  $p_L, \dots, p_{L+R-1}$ ). For this packet  $h[p] \leq (L + R) \gg (n - t) \leq 2^{t-1}$ , therefore, it correctly updates  $c_2$ .

For the induction step, suppose  $c_2 = i \gg (n - t)$  after  $D$  processes packet  $p_i$  updating  $c_2$  and consider the next arrival of packet  $p_j$  to  $D$  that updates  $c_2$ . Fig. 1 partitions the packet sequence at switch  $S$  into groups of  $2^{n-t}$  consecutive packets that have the same synch bits. Let  $I$  and  $J$  denote the groups of  $p_i$  and  $p_j$  respectively. For  $I < J \leq I + \lceil \frac{L+R+1}{2^{n-t}} \rceil$ , Algorithm 1 correctly updates  $c_2$  due to  $\lceil \frac{L+R+1}{2^{n-t}} \rceil \leq 2^{t-1}$ , i.e., the difference between packet header  $h[p_j]$  and  $c_2$  is at most  $2^{t-1}$ . Since at least one packet from the considered sequence of groups arrives to  $D$  after  $p_i$ , no packet from a group later than  $I + 2^t$  arrives first due to  $R$ . By definition of  $j$ , packet  $p_j$  does not belong to groups  $I + 2^{t-1} + 1$  through  $I + 2^t$  because  $D$  does not update  $c_2$  for a packet of these groups.  $J \leq I$  is impossible since conditions (1) imply that  $J \geq I - \lceil \frac{R}{2^{n-t}} \rceil \geq I - \frac{2^{n-1} - 2^{n-t}}{2^{n-t}} > I - 2^{t-1}$ , the difference between  $h[p_j]$  and  $c_2$ 's synch bits is either 0 or greater than  $2^{t-1}$ , and Algorithm 1 appropriately does not change  $c_2$ . This establishes correctness for each update of  $c_2$ .

When flow  $f$  ends,  $c_1$  contains the  $n$  least significant bits of  $|f|$ , and the index of the last packet that updates  $c_2$  differs from  $|f|$  by at most  $L + R + 1$  packets. Since  $L + R + 1 < 2^n$ , Algorithm 1 accounts for all subsequent missing packets

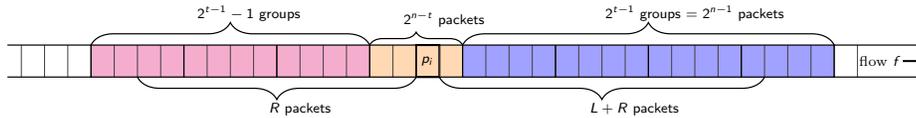


Fig. 1: Packet sequence in the proof of Theorem 1.

when TOTALCOUNT increases  $c_2 \ll (n - t)$  by making its  $n$  least significant bits equal to  $c_1$ . Thus, counter  $c$  correctly computes  $|f|$ .

Parameter  $t$  represents a tradeoff between increasing  $R$  and decreasing  $L$  and  $|f|$ . Without packet reordering, when  $R = 0$ , Algorithm 1 correctly counts packets with loss of up to  $L < 2^{n-1}$  consecutive packets. When  $R > 2^{n-1}$ , Algorithm 1 is never guaranteed to work correctly. Since  $c_2$  never decreases, and  $c_2 \ll (n - t)$  never exceeds the number of packets that have arrived to switch  $S$ ,  $c_2 \ll (n - t)$  can be used as a real-time lower bound on the number of packets arrived to  $S$ .

Algorithm 1 has attractive robustness in practical settings. For example, when a counter chunk contains 12 bits and uses 2 of them as synch bits, Algorithm 1 correctly counts up to  $2^{22}$  packets despite the loss of up to 1023 consecutive packets and reordering stretch up to 1024 packets. Doubling the number of synch bits from 2 to 4 increases the tolerated reordering stretch to 1792 packets, reducing loss tolerance to 255 consecutive packets and decreasing supported flow size to  $2^{20}$  packets.

### 3 Conclusion

In this work, we have studied distributed counter implementation under packet reordering and loss. The basic idea of our design is to exploit the state overlap between two communicating switches to maintain correctness of distributed counter state under network noise.

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